

# Probabilistic Damage Tolerance for Aircraft Fleets Using the FAA-Sponsored SMART|DT Software



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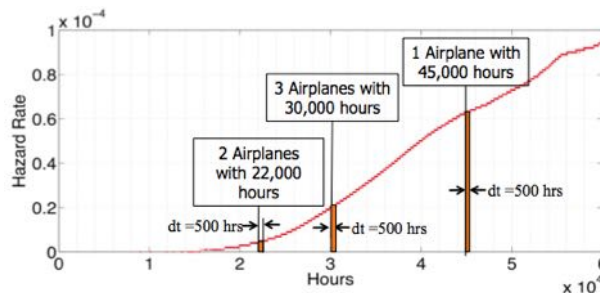
**29th ICAF Symposium – Nagoya, 7–9 June 2017**

# Program Overview

## Fatigue

### Probabilistic Fatigue Analysis for Small Airplanes (SMART<sub>LD</sub>)

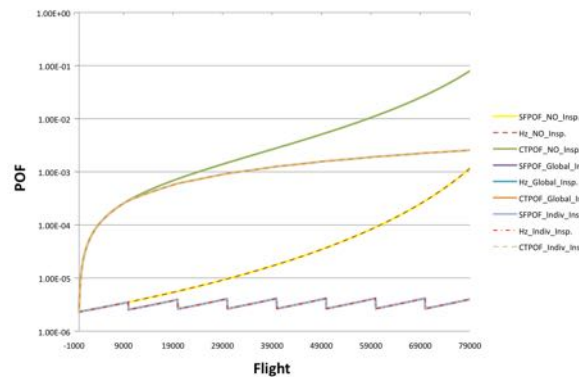
#### Safe-life Approach



- Prob. Life distribution
- Hazard Rate
- Sensitivity Analysis

## Damage Tolerance

### Probabilistic Damage Tolerance Analysis for Small Airplane (SMART<sub>DT</sub>)



- SFPOF, Hz, CTPOF
- Inspection/Repair Effect
- Sensitivity Analysis

### Probabilistic Fatigue Management Program for General Aviation



- Develop experience and familiarity with probabilistic approaches within engineering personnel that design, manufacture and maintain general aviation aircraft.
- Verification with in-service findings.
- Develop a Probabilistically-based fatigue management plan (PFMP) for general aviation

# FAA Support of Probabilistic Fatigue and Damage Tolerance

Contact:

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Federal Aviation Administration

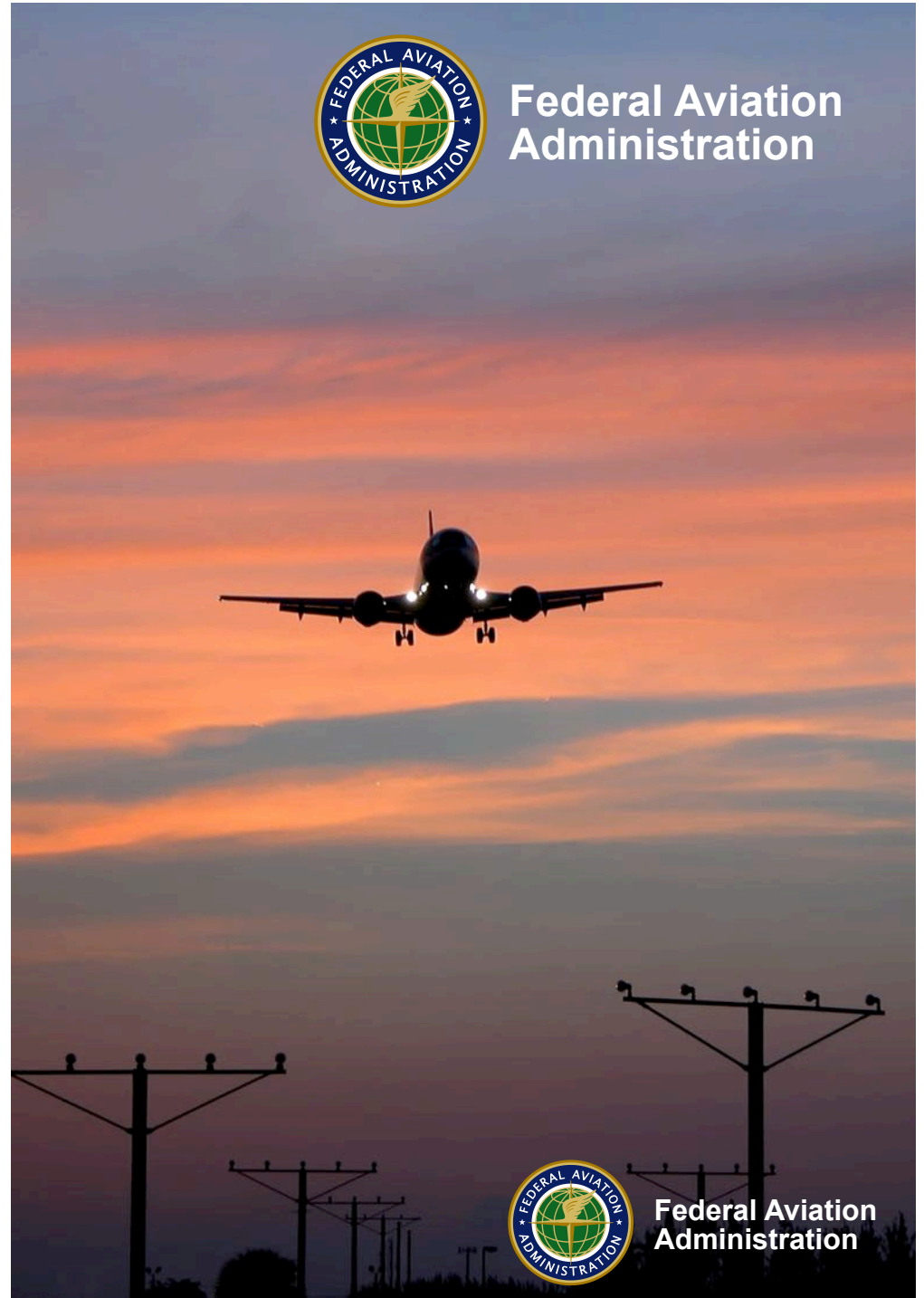
Small Airplane Directorate

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Federal Aviation  
Administration



Federal Aviation  
Administration

# FAA Interest in Probabilistic Fatigue/DT

- **FAA Order 8110.107A Monitor Safety/Analyze Data (MSAD) (10/1/2012)**
  - FAA will use quantitative risk analysis in making continued operational safety decisions. (Airworthiness Directives)
- **Order has effect of requiring probabilistic methods when applicable.**



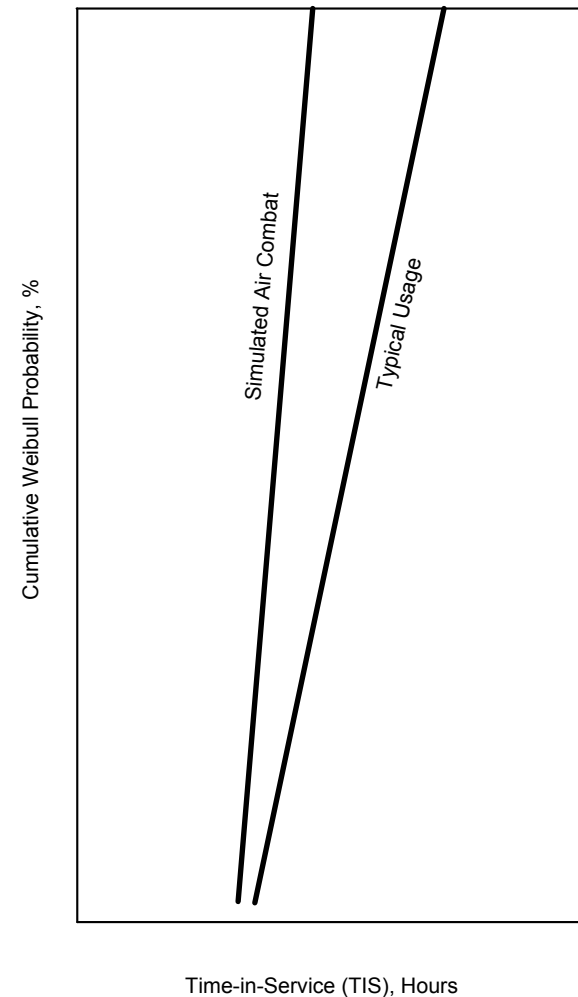
# FAA Interest in Probabilistic Fatigue/DT

- **Even before the Order was published, FAA Small Airplane Directorate (SAD) was adopting probabilistic methods.**
- **Airworthiness Directive for Cessna 402**
  - Spar cracking with critical crack size less than detectable crack size
  - Large percentage of fleet older than 'life-limit' solution, would have caused groundings
  - Used risk management to schedule modifications considering time-in-service and modification resources.



# FAA Interest in Probabilistic Fatigue/DT

- **SAD often deals with diverse fleet usage**
  - Minority sub-fleet operated with more severe stress spectrum than remainder of fleet
  - Relative risk between different stress spectra
  - Insight into how to manage risk within constraints of 14 CFR Part 39 Airworthiness Directives



# FAA Interest in Probabilistic Fatigue/DT

- **Revision of AC 23-13**
  - Review historical guidance (AFS-120-73-2)
    - Why scatter factor = 4.0?
    - Why gust and maneuver spectra offset by 1.5 standard deviations?
    - ‘Deterministic’ solution to probabilistic problem
  - Used Monte Carlo simulations to validate
    - ‘Probability Basis of Safe-Life Evaluations in Small Airplanes’, 9<sup>th</sup> Joint FAA/DoD/NASA Aging Aircraft Conference
    - SMART<sub>LD</sub> gives expanded capabilities to in-house FAA Monte Carlo simulations



# FAA Interest in Probabilistic Fatigue/DT

- **SMART<sub>LD</sub> and SMART<sub>DT</sub> gives the FAA the capability to use probabilistic fatigue/DT to:**
  - Update regulations, policy, and guidance
  - Evaluate unsafe conditions and design corrective actions

## Additional Questions:

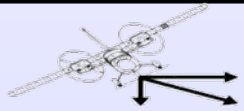
- **How can the SMART Technology be used in transport Airplanes?**
- **How to incorporate this technology for early stages of the airplane life (Also for design, not only airworthiness,)**



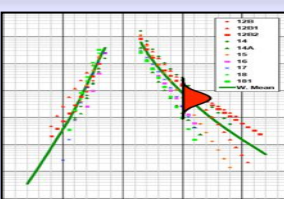


## Loading Data

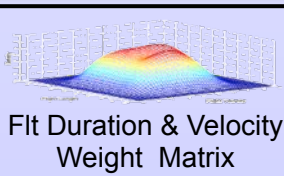
Internally Generated Loading



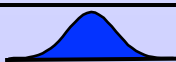
Load Limit Factors



Exceedance Curves

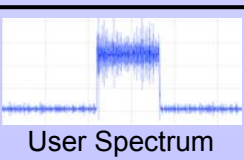


Flt Duration & Velocity Weight Matrix



Sink Rate

User Loading

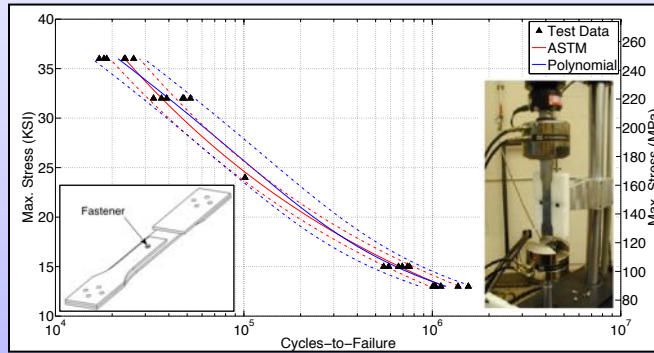


User Spectrum



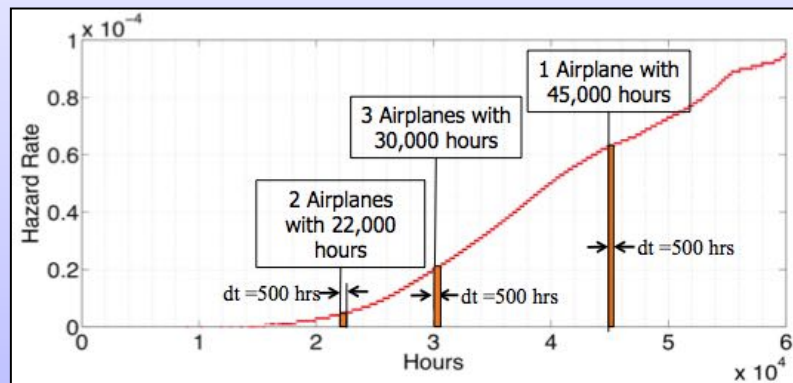
Stress Mult. Factor

## Probabilistic SN Data



- Internal libraries from test results
- FAA AC23-13A
- User Defined

## Monte Carlo Sampling



Random Damage Index

Miner's Coefficient



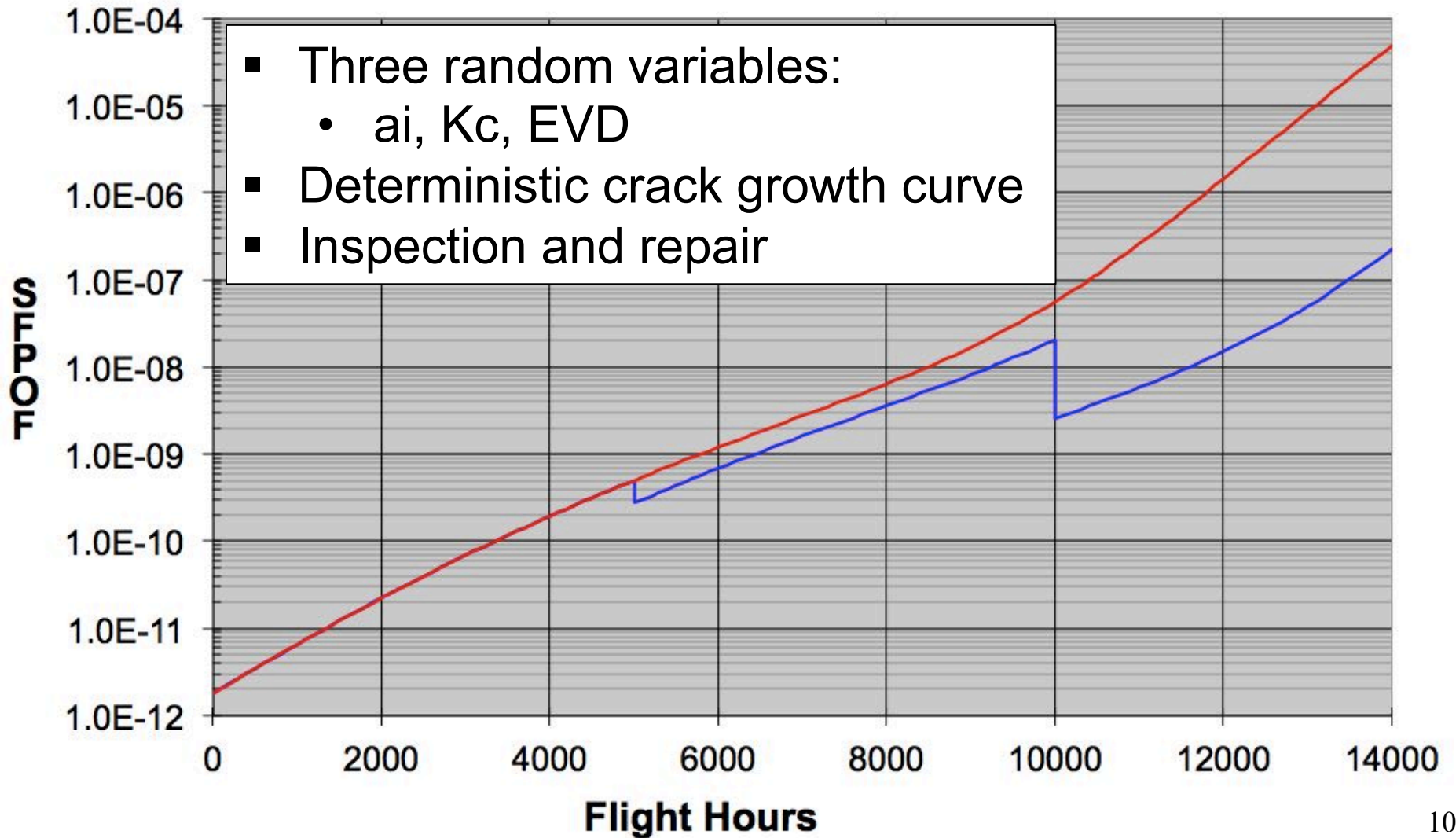
Life Distribution

Sensitivities

Currently Available



# Previous S-O-T-A



# Development Philosophy

- Run any crack growth model



- Consider any repair scenario



Oversized Hole

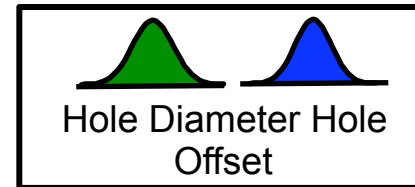
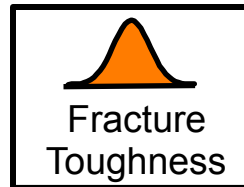
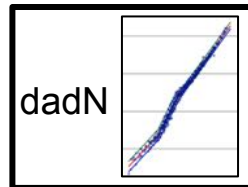
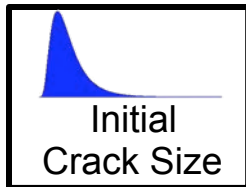


Doubler



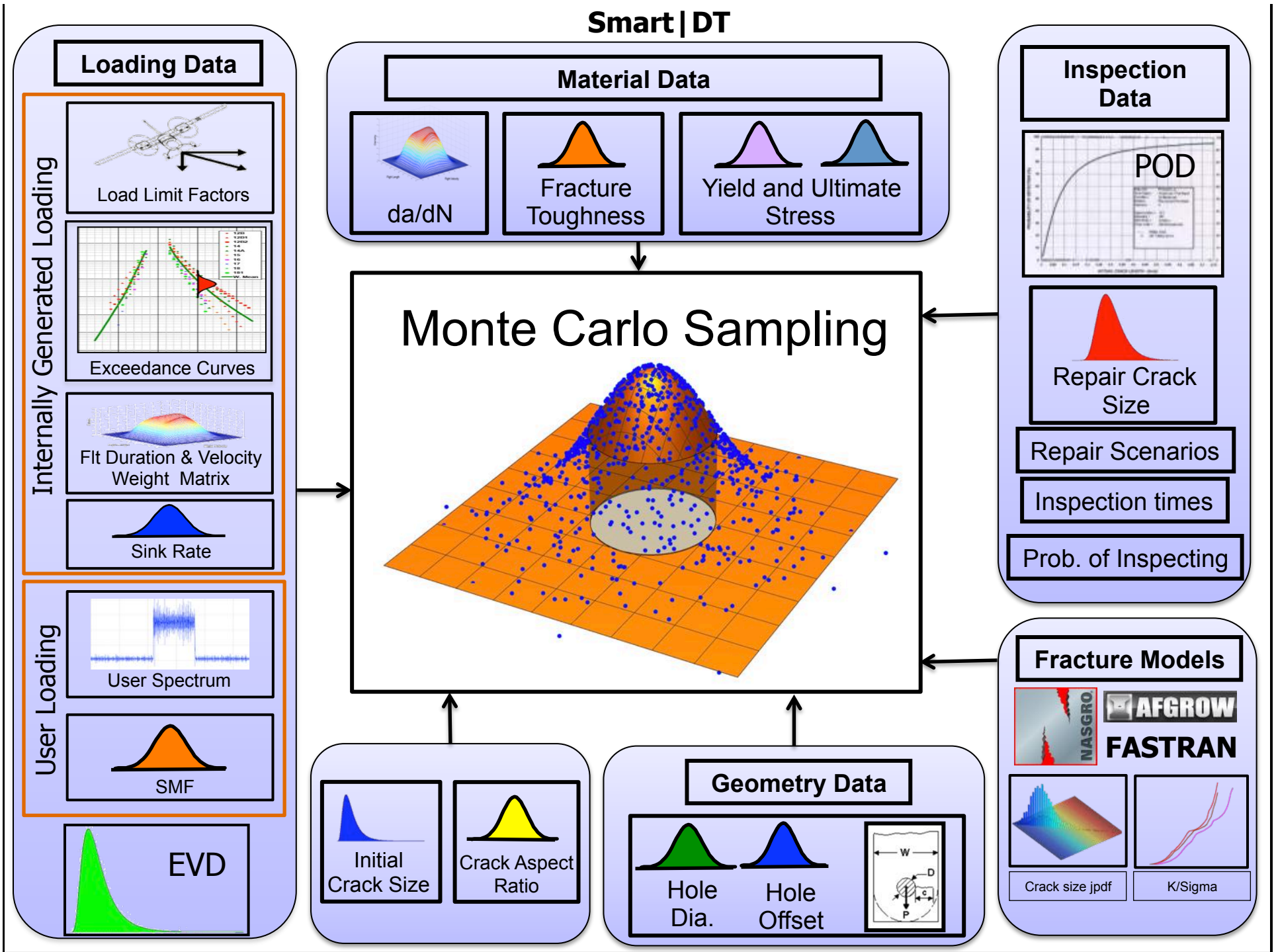
Replacement

- Consider any random variable



Etc.

# Smart | DT



# Probability Equations

The probability-of-failure is the probability that maximum value of the applied stress (during the next flight) will exceed the residual strength  $\sigma_{RS}$  of the aircraft component

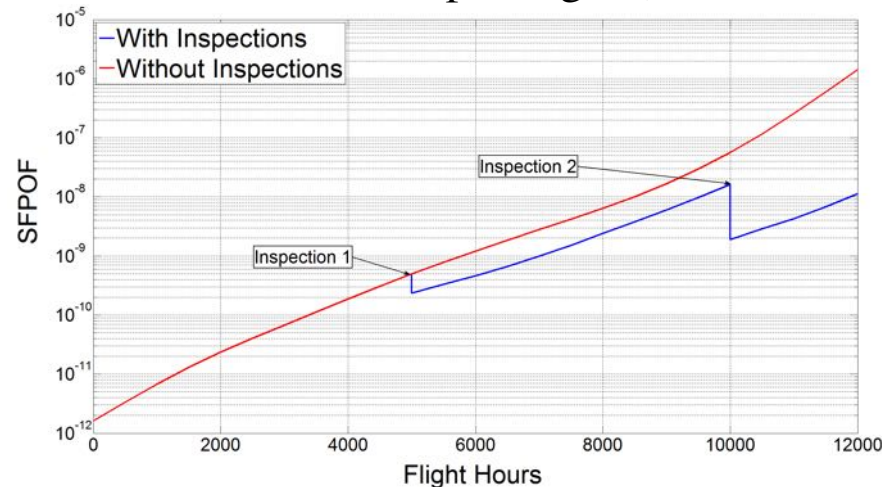
$$POF_{\text{no-surv}}(t) = P[\sigma_{Max} > \sigma_{RS}(t)] = \int [1 - F_{EVD}(\sigma_{RS}(t))] f_{\mathbf{x}}(\mathbf{x}) d\mathbf{x}$$

$$CTPOF(t) = \int \left[ 1 - \prod_{i=1}^t F_{EVD}(\sigma_{RS}(t_i)) \right] f_{\mathbf{x}}(\mathbf{x}) d\mathbf{x}$$

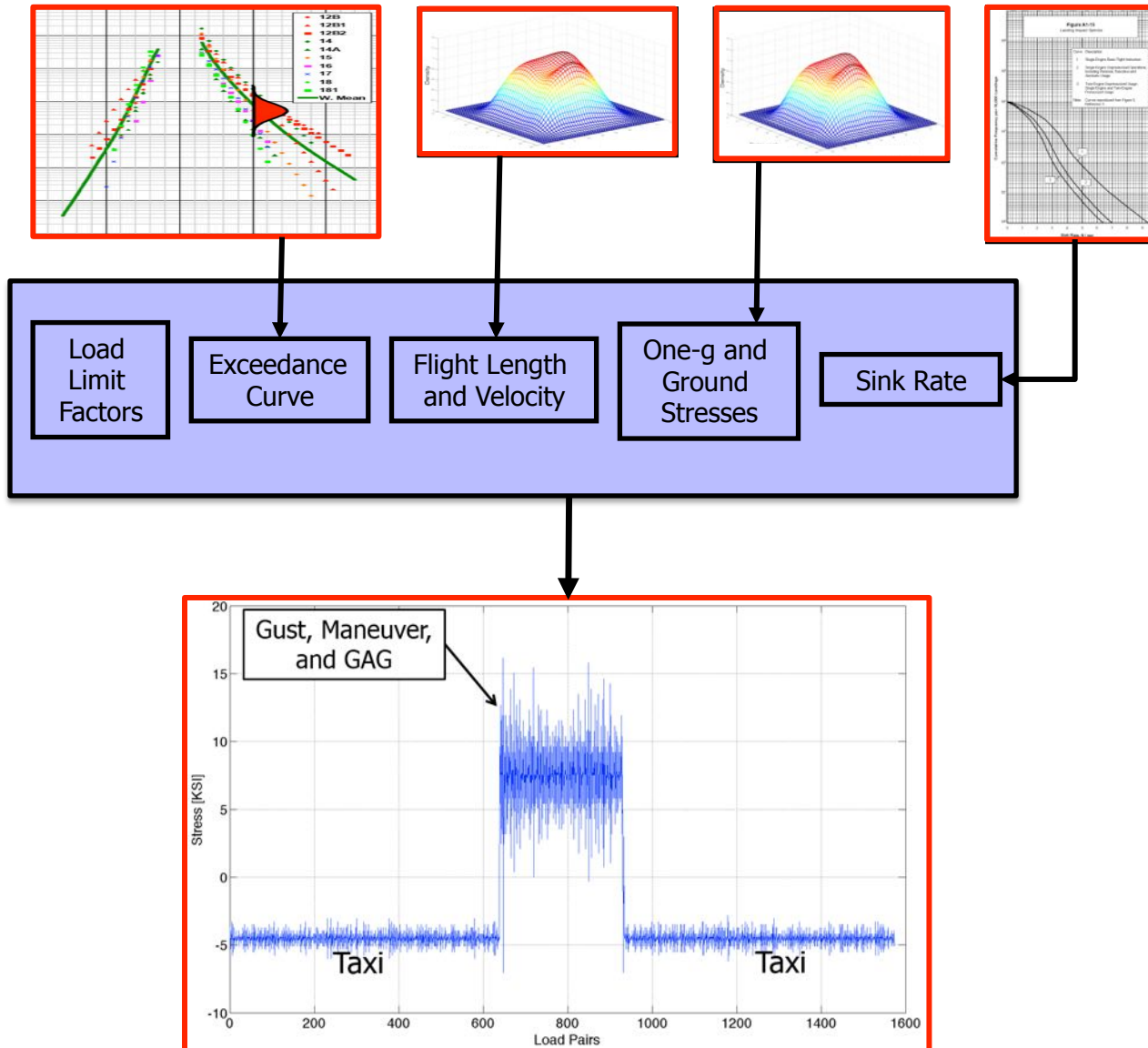
$$POF_{\text{surv}}(t) = \int \left[ \prod_{i=1}^{t-1} F_{EVD}(\sigma_{RS}(t_i)) \right] [1 - F_{EVD}(\sigma_{RS}(t))] f_{\mathbf{x}}(\mathbf{x}) d\mathbf{x}$$

$$Hz(t) = \frac{POF_{\text{surv}}(t)}{1 - CTPOF(t)}$$

$F_{EVD}$  = CDF of maximum stress per flight (extreme value distribution).



# Spectrum Generation

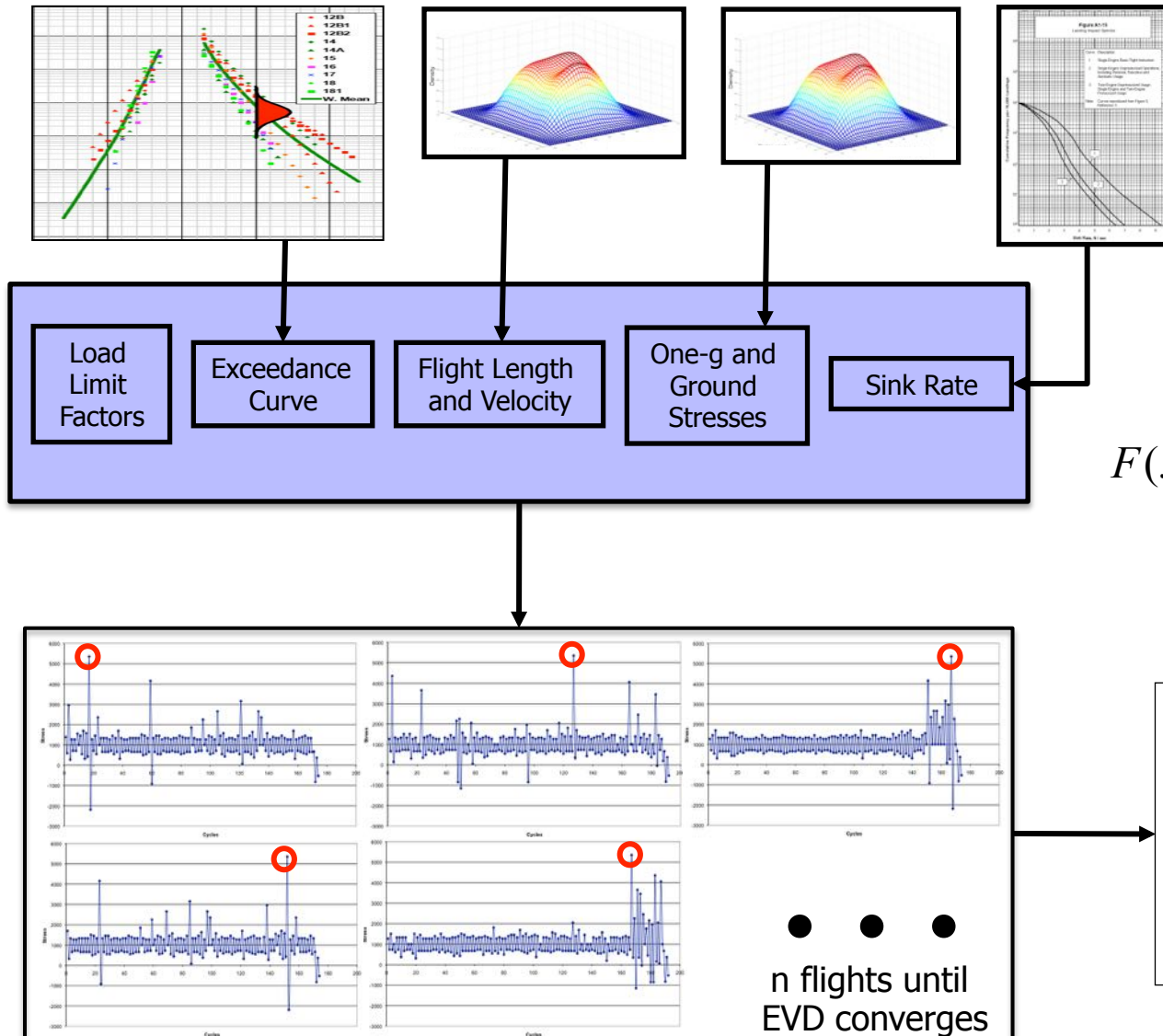


- ✓ Exceedance curves
  - ✓ internal and user-defined
- ✓ Mixed usages
- ✓ Flight duration and weight matrices random to simulate flight profiles and different operations
- ✓ Randomized flights and stresses
- ✓ Spectrum editing options
- ✓ User-defined spectra
  - ✓ Afgrow format

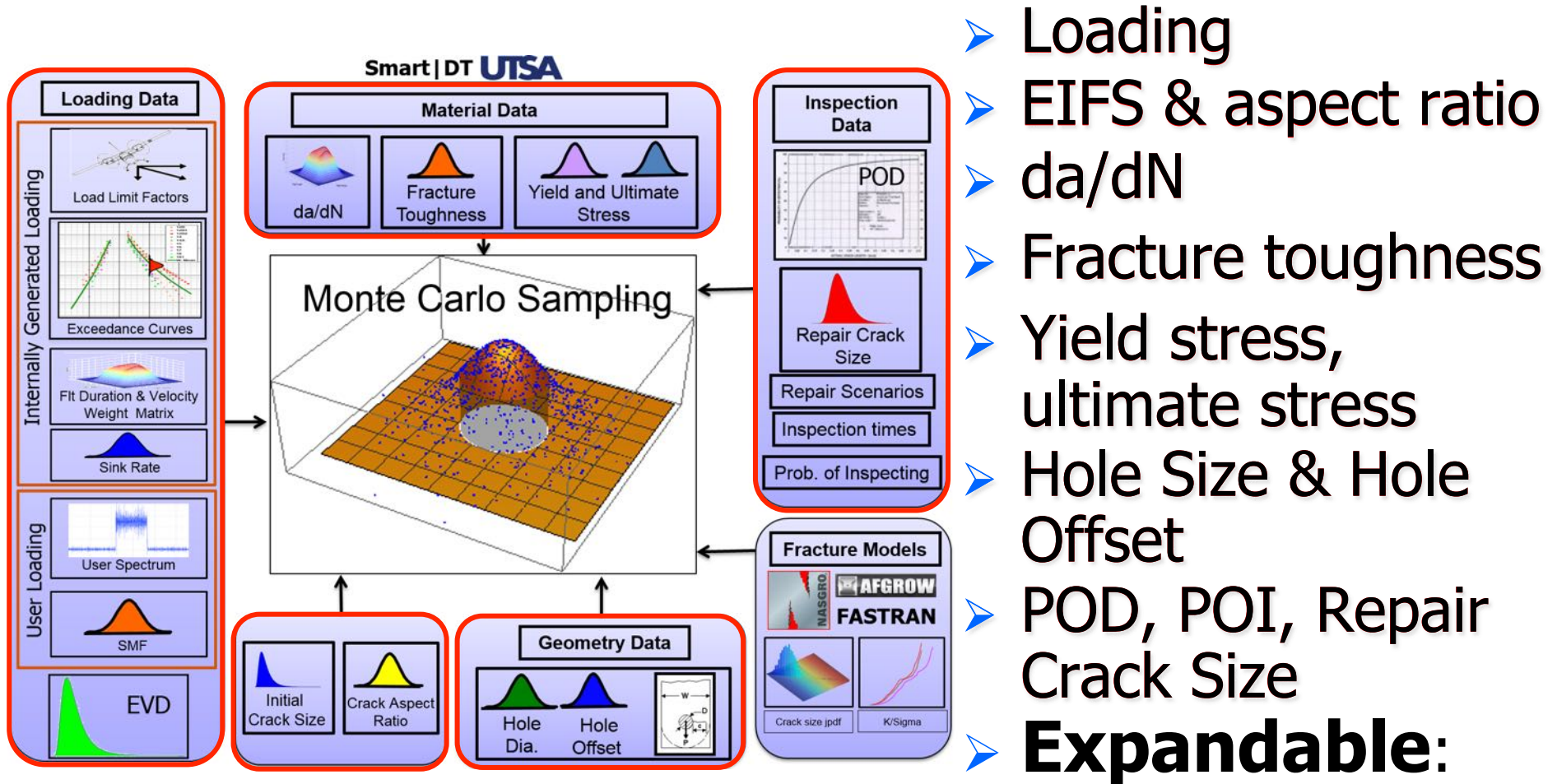
# EVD Generation

✓ EVD computed internally from spectrum

$$F(x) = \exp \left\{ - \left[ 1 + \xi \left( \frac{x - \mu}{\sigma} \right) \right]^{-1/\xi} \right\}$$

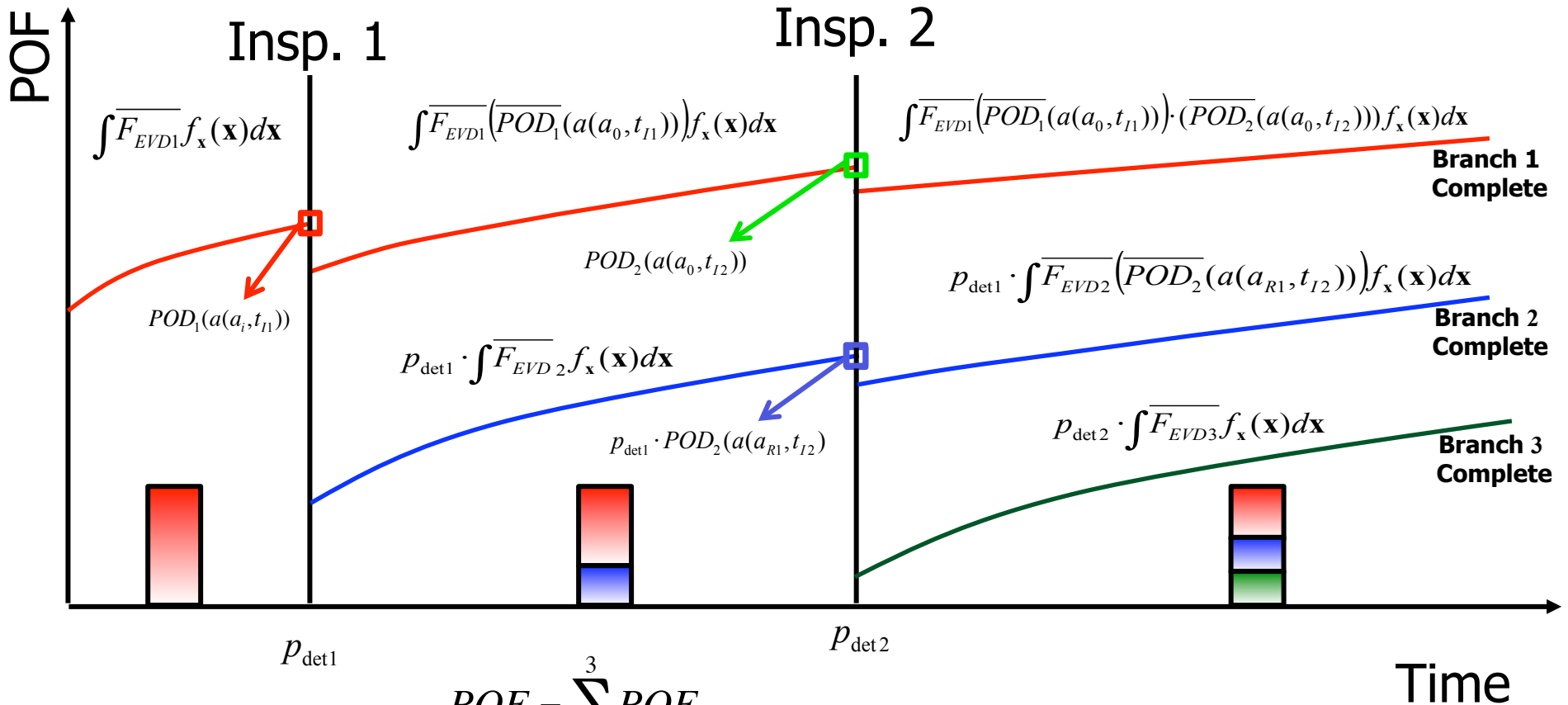


# Comprehensive Random Variables





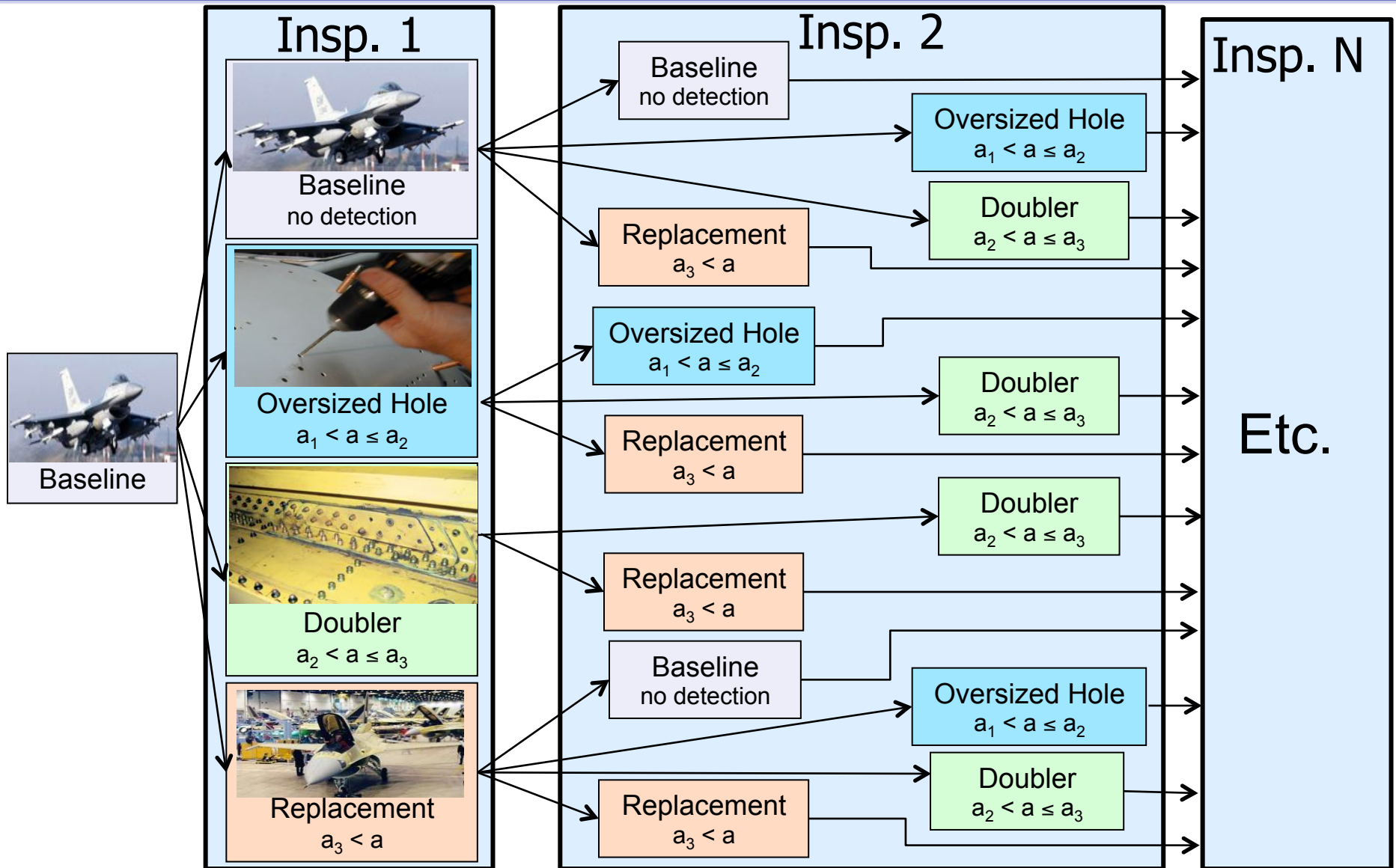
# Multiple Inspections



Add the contribution from each branch into the final POF

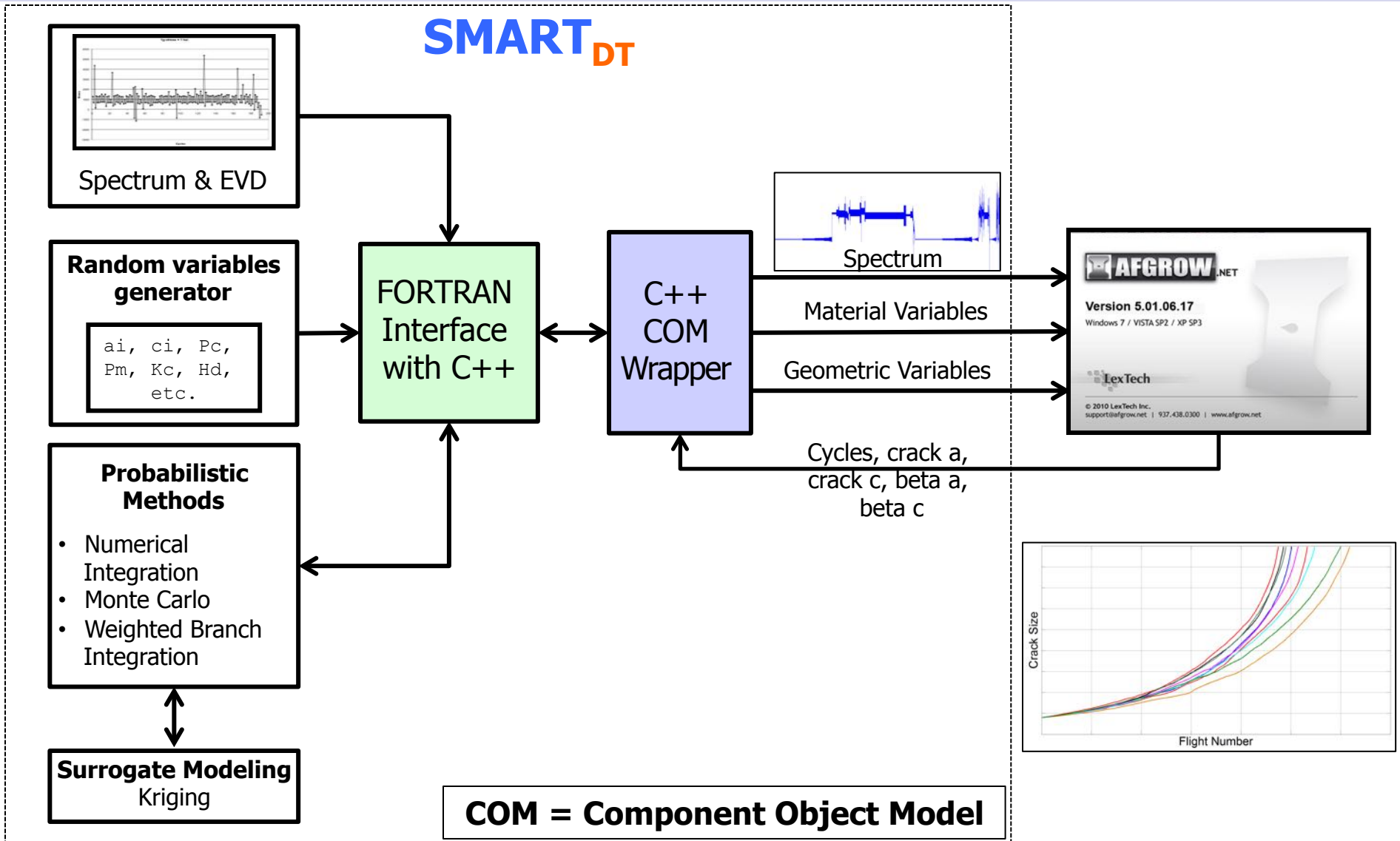


# Multiple Repair Example (Future Version)



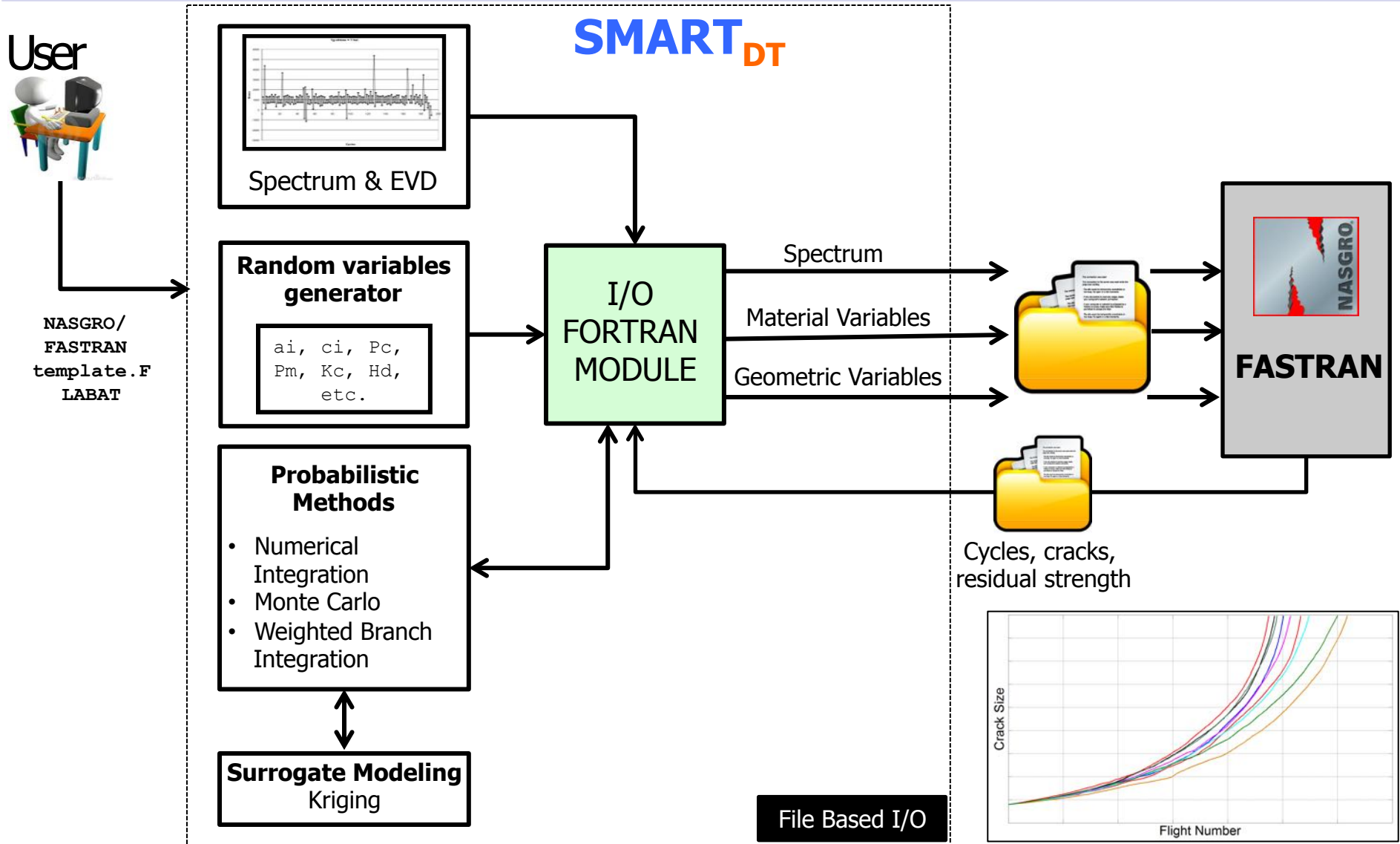


# AFGROW Interface: COM driven





# FASTRAN/NASGRO Interface Runs in Parallel



# Kriging Surrogate Model

- Efficient Method to compute Crack Size (a) and Residual Strength (RS).
  - Train surface with crack growth analyses.

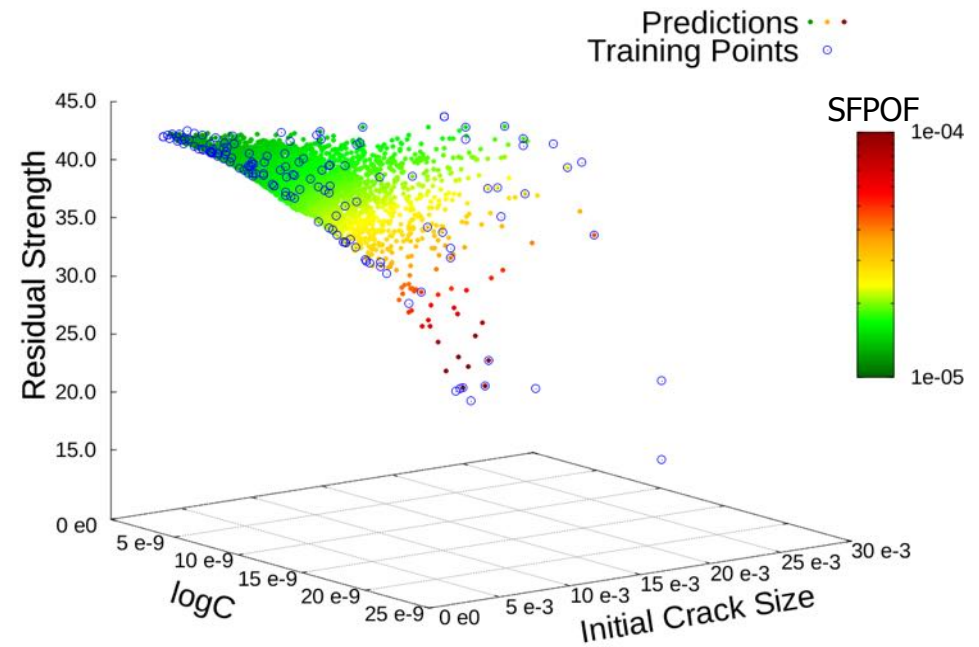
$$\frac{\partial a}{\partial N} = f(\Delta K, a, c)$$

$$\frac{\partial c}{\partial N} = f(\Delta K, a, c)$$

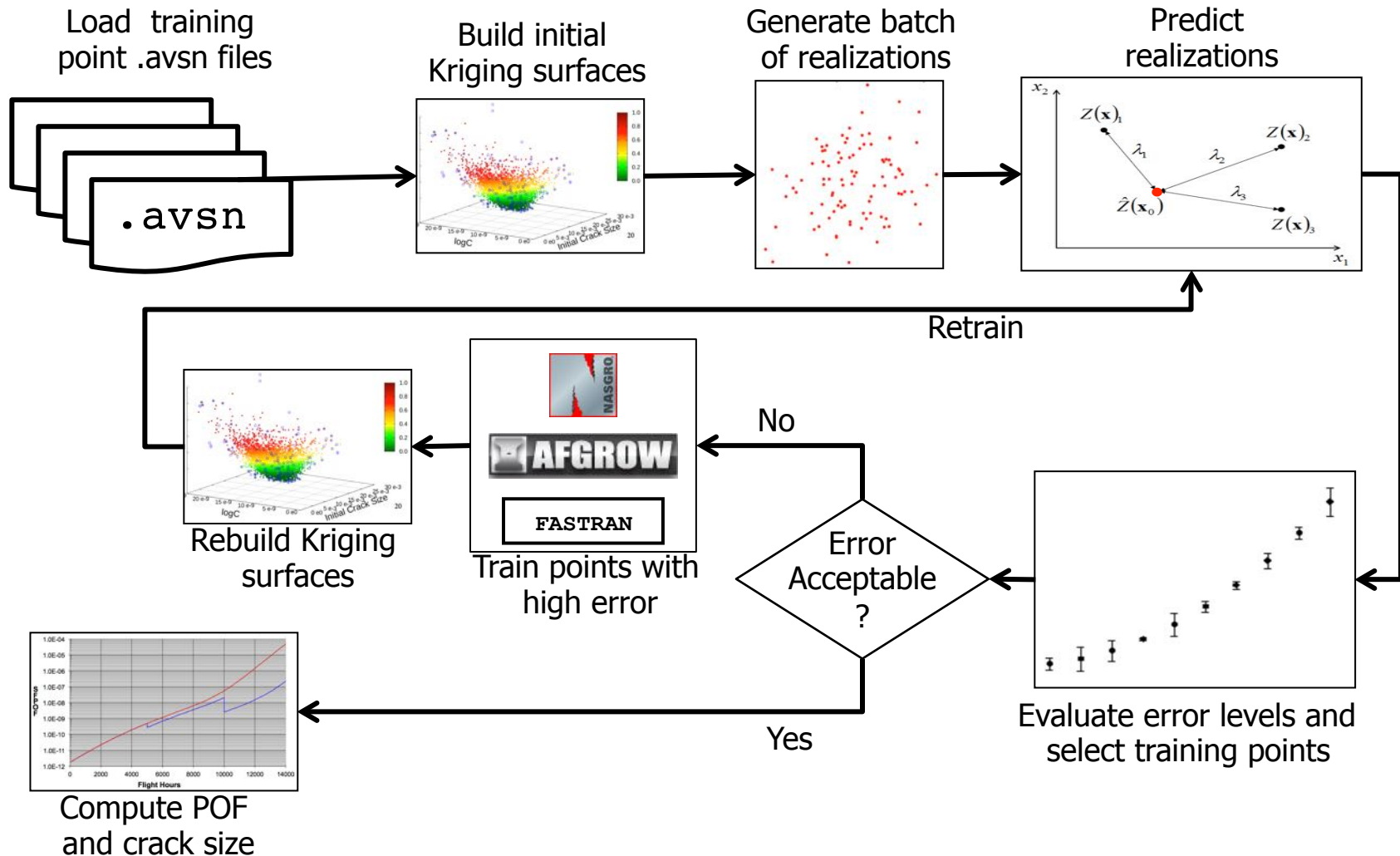


$$f(x) + Z(x)$$

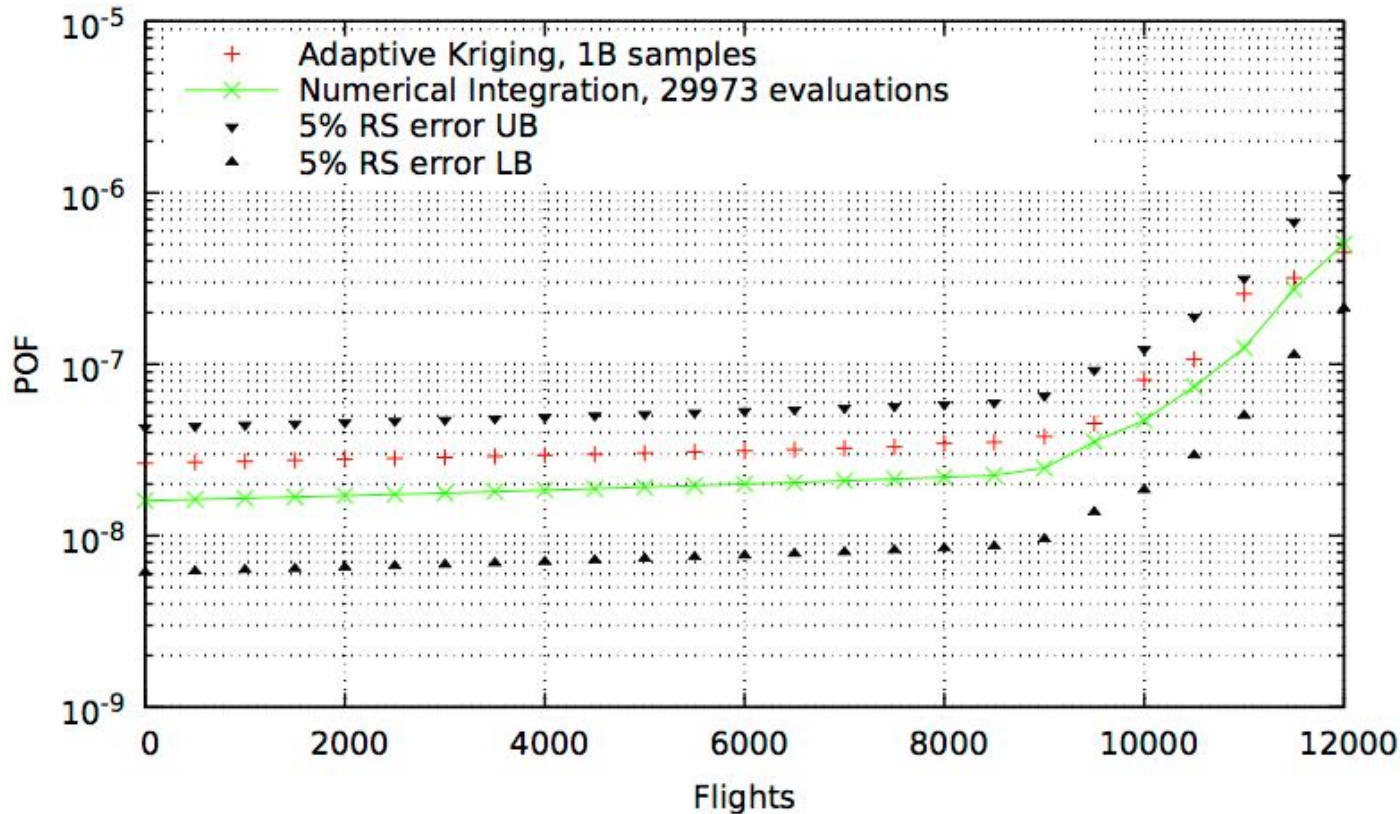
- After building the Kriging surface predict “a” and “RS”.



# Adaptive Surrogate Model Error Reduction



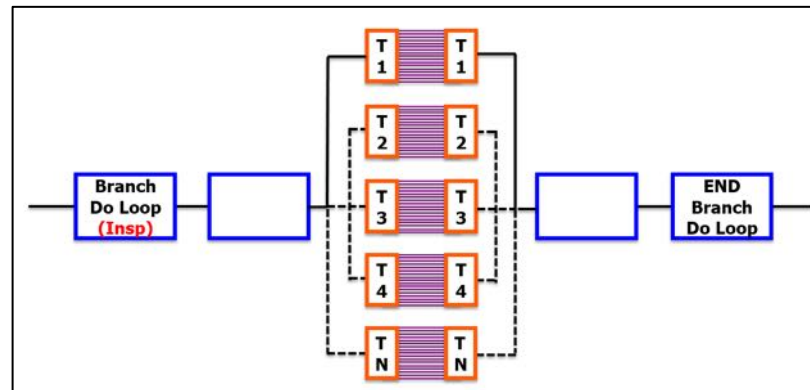
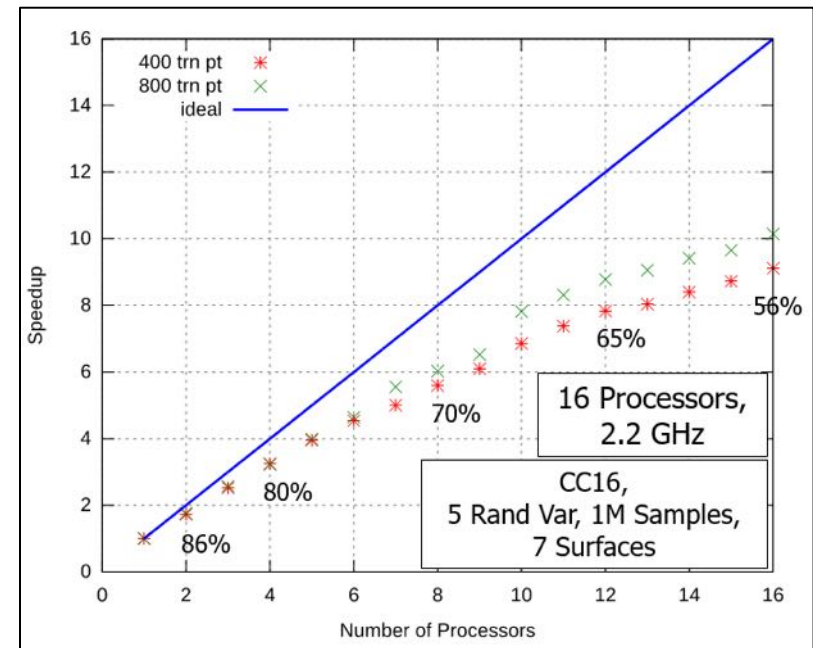
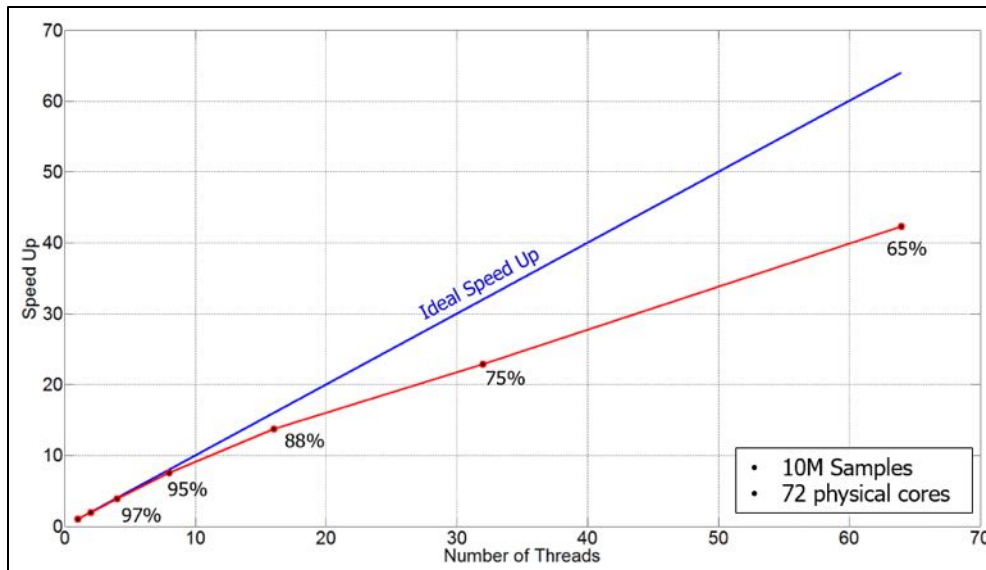
# Paper Example Problem



Kriging predictions are within 5% residual strength error bounds indicated

6 RVs:  $a_i$ ,  $k_c$ ,  $\rho$ ,  $c$ ,  $\phi_{\text{hole}}$ , edge dist,  $\sigma_{\text{max}}$   
 128 initial training points  
 921 additional training points  
 Runtime 8.5 hours on 16 processors

# Parallel & Vectorized (Master Curve)



Identical Results wrt threads and operating system

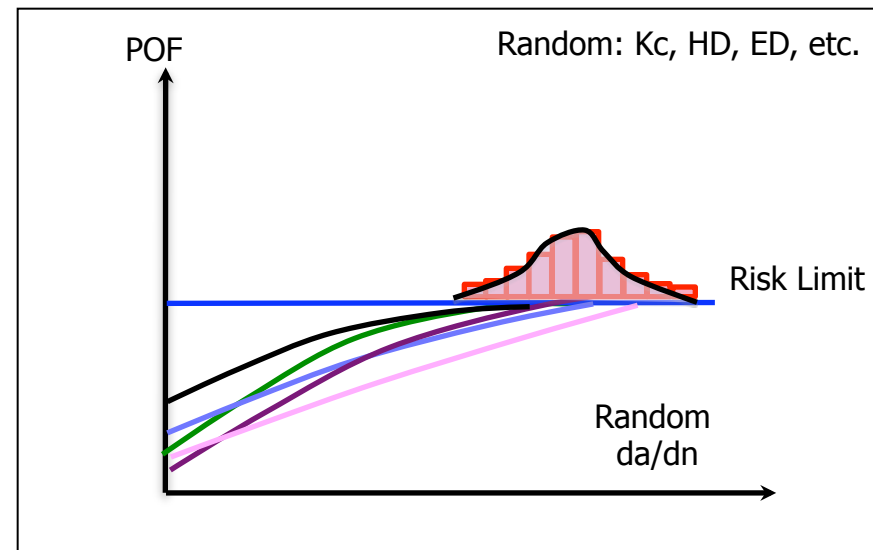
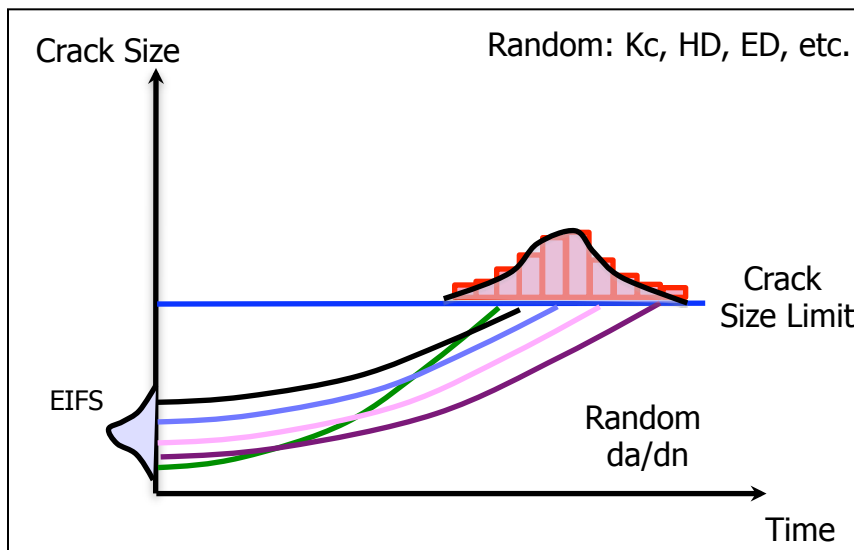




# Remaining Useful Life Calculations



SMART drives the fracture mechanics analysis to an user-defined crack length or the probabilistic calculations to an user defined risk level



## Applications:

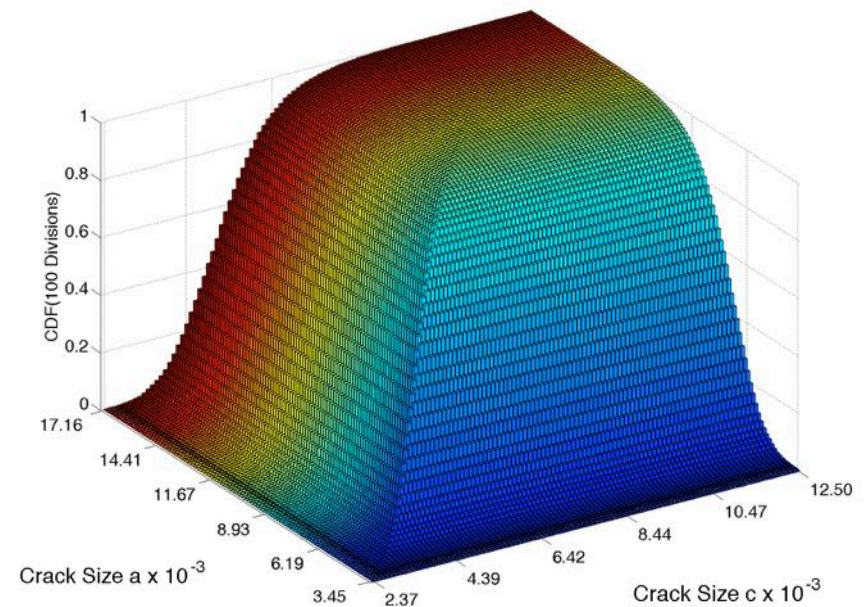
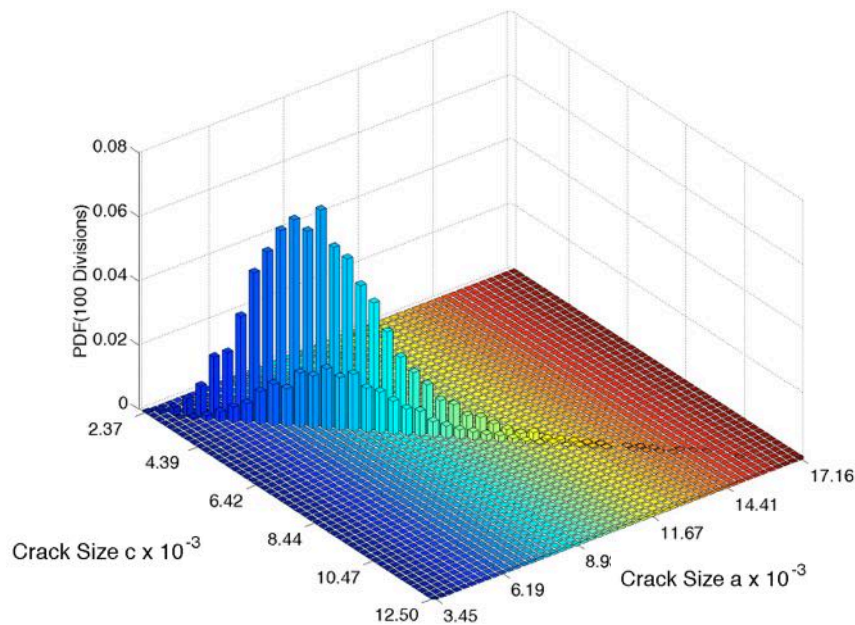
- Largest crack size that can be drilled out in a CP location
- Crack size corresponding to a crack that has a 90% chance of being found, with 95% confidence, with NDI



# Crack Size Distributions



Both “a” and “c” crack tips tracked through time.  
Joint distribution computed.

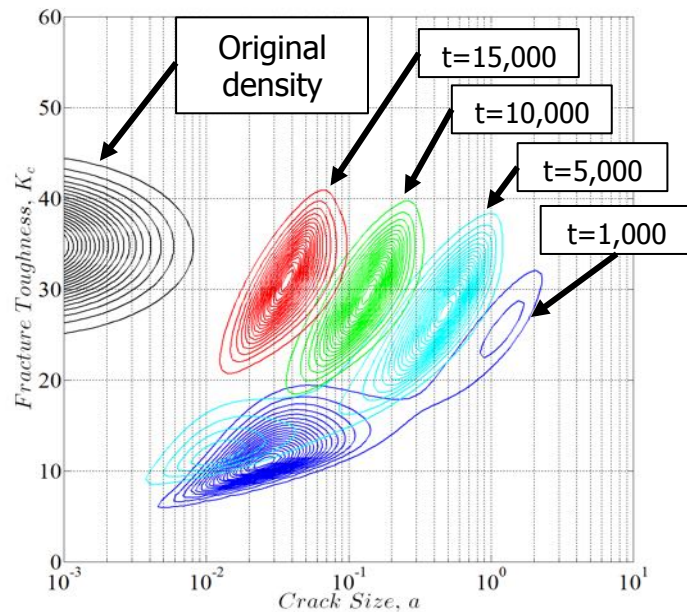


Crack Size at time = 5000

# Advance Sampling Methods

Optimal parameters for the random variables to efficiently compute the probability of failure.

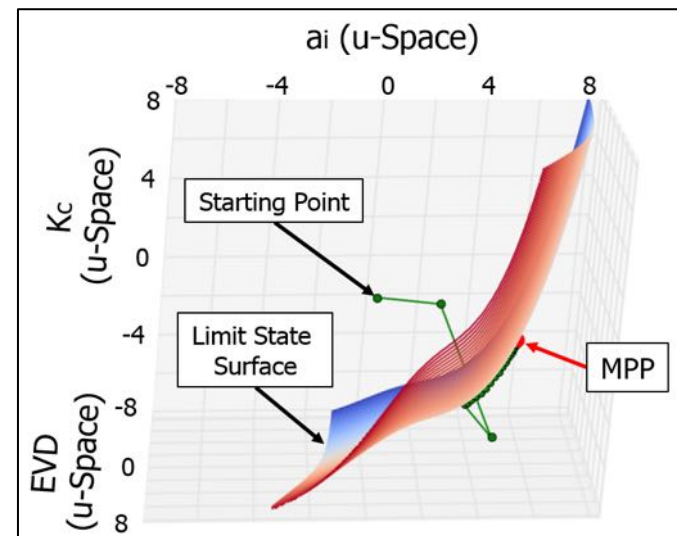
$$POF = \int_{-\infty}^{\infty} [1 - F_{max}(\sigma_{RS})] \frac{f_X(x; u)}{q_X(x; v^*)} q_X(x; v^*) dx$$



Imp. Sampling  $-a_i$  and  $K_c$

Fast approximate method to compute low POF values

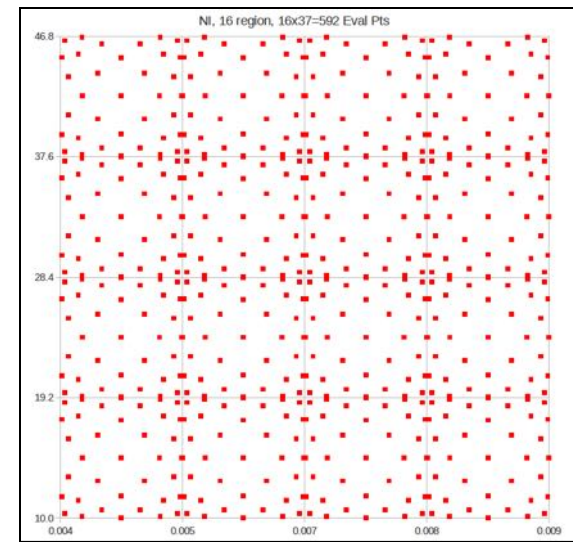
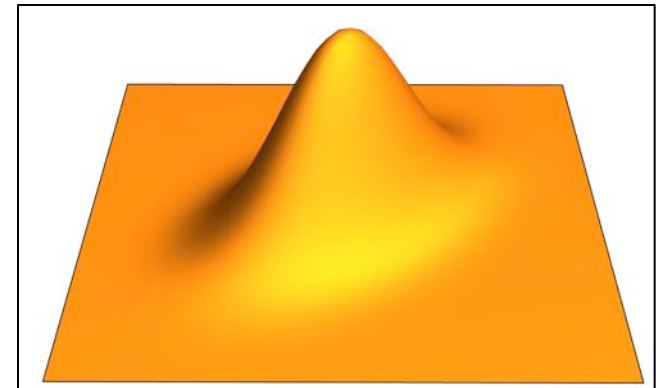
$$POF = \Phi(\beta)$$



Most Probable Point (MPP)

# Numerical Integration

- Adaptive numerical integration.
  - Adaptive strategies
  - Error estimates
  - Specify number of evaluations
  - Specify error
  - High dimensional integrals





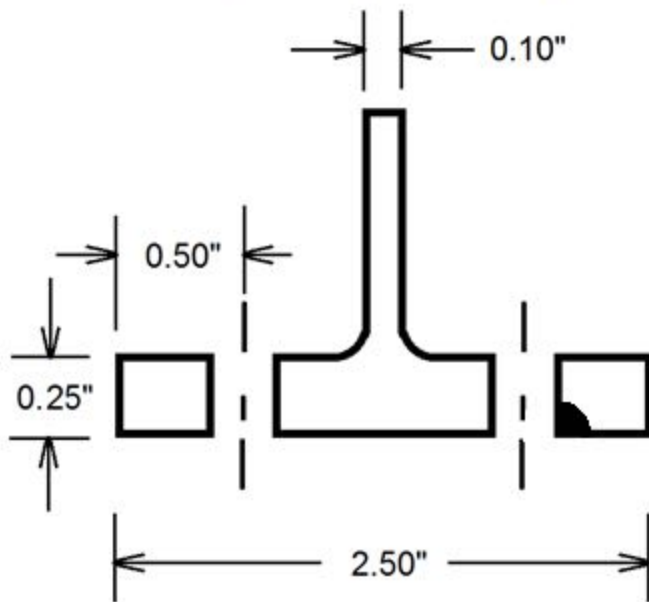
# Example Problem Overview



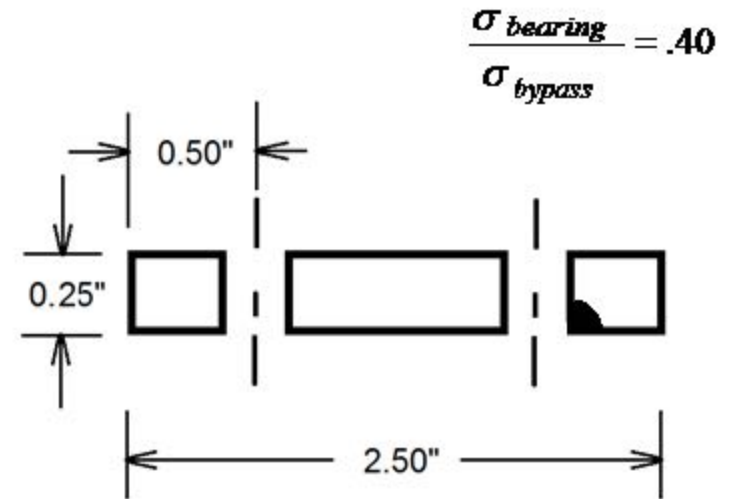
Twin engine unpressurized airplane with a history of fatigue cracks in the wing spar cap

# Problem Overview

Spar Cap Geometry



Idealized Geometry



## Deterministic Variables

## Value

Hole radius	0.156 in
Cap Thickness	0.250 in
Cap Width	2.50 in



# Problem Overview



<b>Loading Parameters</b>	<b>Value</b>
Aircraft Usage	Twin Engine Unpressurized General Usage
Design Maneuver Load Factors	3.60 (high)
	-1.50 (low)
Design Gust Load Factors	4.50 (high)
	-2.50 (low)
Ground Stress	-50 psi (Flight 1)
	-70 psi (Flight 2)
One g Stress	9500 psi (Flight 1)
	8800 psi (Flight 2)
Average Velocity	200 knots (Flight 1)
	200 knots (Flight 2)
Number of Flight Times	1 (Flight 1)
	1 (Flight 2)
Number of Velocities	5 (Flight 1)
	5 (Flight 2)



# Problem Overview



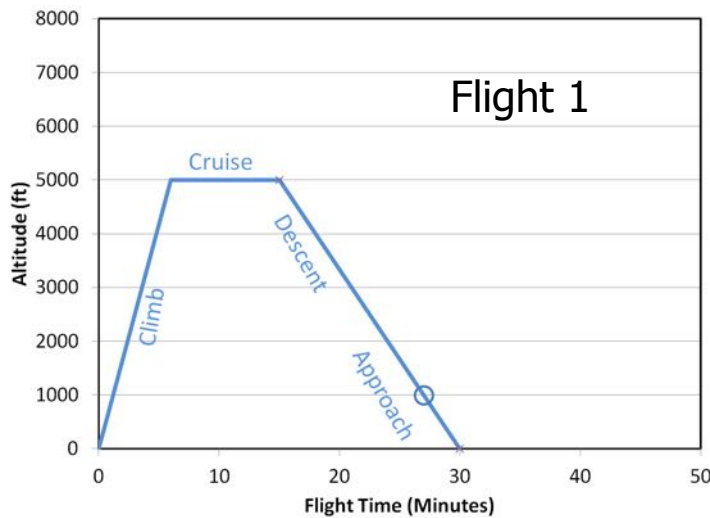
Random Variables	Distribution	Parameters
Initial Crack Size	Lognormal	Mean = 0.005 in Standard deviation = 0.002 in
Fracture Toughness	Normal	Mean = 35.0 ksi√ in Standard deviation = 1.1 ksi√ in
Paris m	Binormal	Mean = 3.80 Standard deviation = 0.04
Paris c (log)	Binormal	Mean = -9.00 Standard deviation = 0.04
Ultimate Stress	Normal	Mean = 80.0 ksi Standard deviation = 3.0 ksi
Yield Stress	Normal	Mean = 65.0 ksi Standard deviation = 2.0 ksi
Hole Offset	Normal	Mean = 0.50 in Standard deviation = .025 in

Other Parameters	Distribution
Crack Growth Program	NASGRO





# Define Flight Matrices



Segment	Weight	KEAS	% Duration
CLIMB	6580	140	0.20
CRUISE	6440	160	0.50
DESCENT	6300	180	0.20
APPROACH	6160	120	0.10

$V_C = 200 \text{ KEAS}$

$MTOW = 7000 \text{ lb}$

Sort matrix in ascending order for speed & weight

Average Speed During Flight, % Max Takeoff Weight

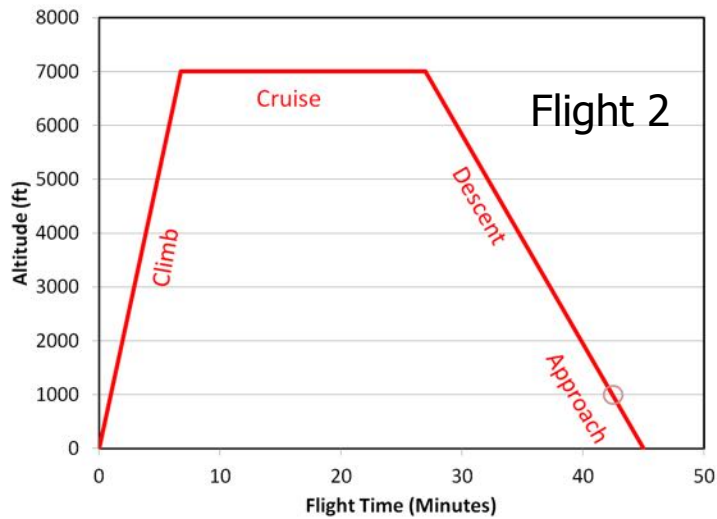
Flight Time (hrs)	% of Flights	0.88	0.90	0.92	0.94	0.96
0.5	1.0	0.10	0.20	0.50	0.20	0.0

Average Speed During Flight, % Design Velocity

Flight Time (hrs)	% of Flights	0.60	0.70	0.80	0.90	1.00
0.5	1.0	0.10	0.20	0.50	0.20	0.0



# Define Flight Matrices



Segment	Weight	KEAS	% Duration
CLIMB	6720	140	0.15
CRUISE	6580	160	0.60
DESCENT	6440	180	0.15
APPROACH	6300	120	0.10

$$V_C = 200 \text{ KEAS}$$

$$\text{MTOW} = 7000 \text{ lb}$$

Sort matrix in ascending order for speed & weight

Average Speed During Flight, % Max Takeoff Weight

Flight Time (hrs)	% of Flights	0.80	0.90	0.92	0.94	0.96
0.75	1.0	0.0	0.10	0.15	0.60	0.15

Average Speed During Flight, % Design Velocity

Flight Time (hrs)	% of Flights	0.600	0.70	0.80	0.90	1.00
0.75	1.0	0.10	0.15	0.60	0.15	0.00



# Problem Overview



<b>Inspection Parameters</b>	<b>Value</b>
Number of Inspection Types	One - Single Repair
Inspection Type	Eddy Current
Inspection Schedule	14,000 Hour Initial 2,000 Hour Repetitive
Probability of Inspection	80%
Probability of Detection	Deterministic
Detectable Crack Size	.06 inch
Repair Crack POD	Deterministic
Repair Crack Size	.01 inch

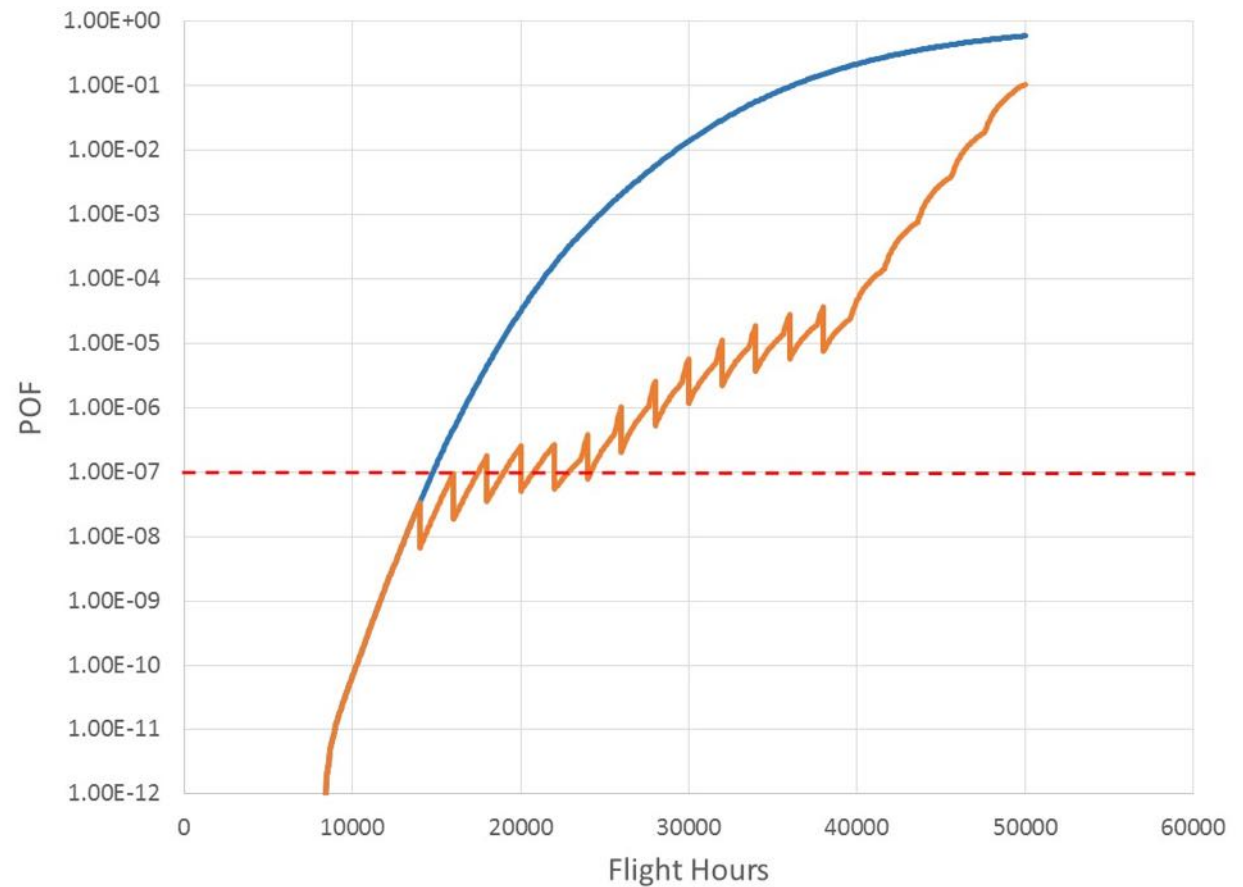


# Plot POF



## Summary

- POF  $> 10^{-7}$
- Start inspections 2000 hours later
- Reduce inspection to 1000 hours



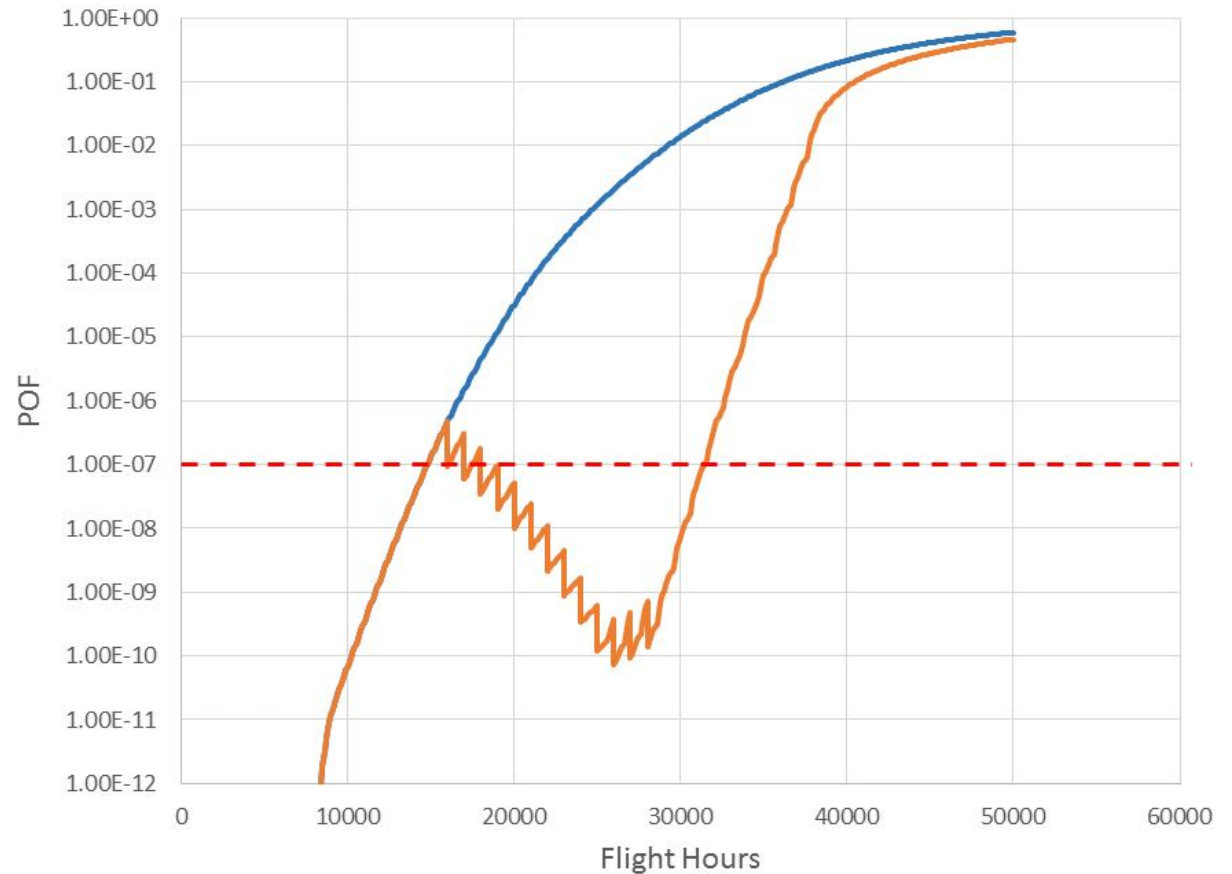


# Plot POF



## Summary

- Corner Crack
- Master Curve
- Nasgro
  - CC16
- Random Variables
  - Initial Crack Size





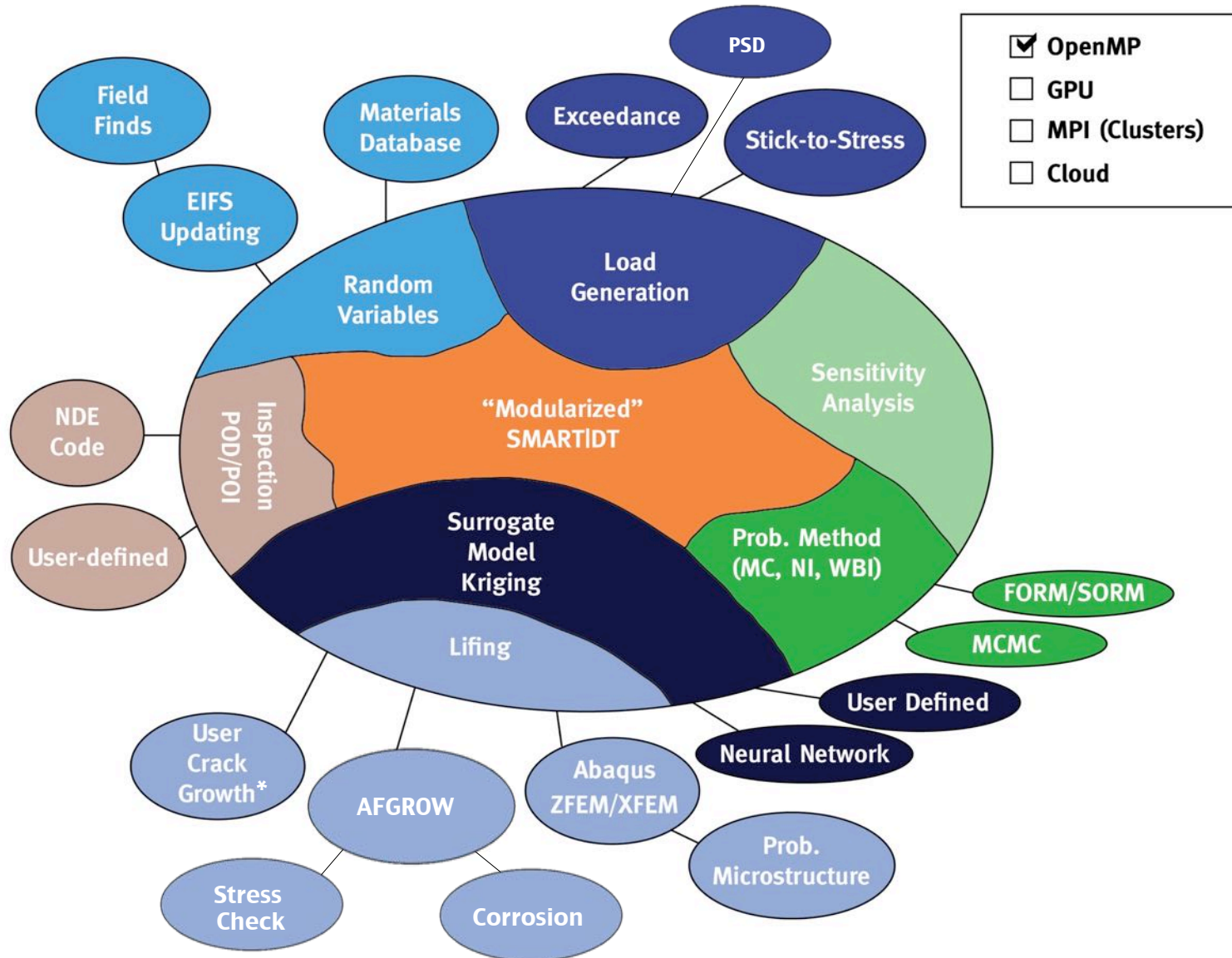
# Future-Current Work



- Development of an internal probabilistic data base
- Development of an internal crack growth
- Advance sampling methods
- Probabilistic Residual Stresses
- PDTA on composites
- Risk based inspections
- Development of training material



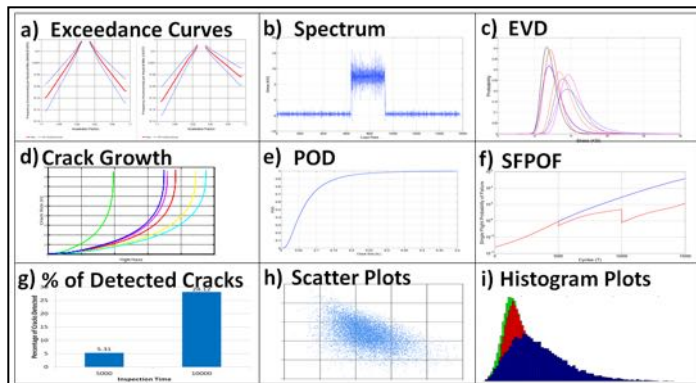
# Plays well with Others



# Code Availability

- For more information contact:
  - [jocampo@stmarytx.edu](mailto:jocampo@stmarytx.edu)
  - [harry.millwater@utsa.edu](mailto:harry.millwater@utsa.edu)

<http://smart-software.utsa.edu>



## SMART Risk Assessment



Under sponsorship from the Federal Aviation Administration (FAA)\*, the University of Texas at San Antonio (UTSA) has developed a software suite to assist engineers in performing risk assessments of aircraft structures. Two software products are available: SMART|LD (probabilistic S-N), and Smart|DT (probabilistic damage tolerance). SMART|LD considers classic fatigue failure with probabilistic loading, S-N curves, Stress Severity Factor (SSF), and option for user defined spectra and SN Curves. SMART|DT considers explicit crack growth with probabilistic loading, fracture toughness, da/dN material data, initial crack sizes, geometry, and inspection capabilities. Interfaces to Aifrow, Nasgro, and Fastran are available. Training material is provided at this web site and at relevant conferences. The software programs are to be considered beta and regularly updated by UTSA.





# Acknowledgements



- Probabilistic Damage Tolerance-Based Maintenance Planning for Small Airplanes, Sep. 2009-Aug. 2012, Federal Aviation Administration, Grant 09-G-016
- Probabilistic Fatigue Management Program for General Aviation, Sep. 2012-Aug. 2016, Federal Aviation Administration, Grant 12-G-012
  - Sohrob Mattaghi (FAA Tech Center) – Program Manager
  - Michael Reyer (Kansas City) - Sponsor

# Smart|DT Capabilities

- Loading Generation
  - Computed from exceedance curves (Internal library and user exceedance option) – Weighted usage available.
  - Flight Duration and weight matrices, Design load limit factors, one-g stress, and ground stress as user input.
  - Stresses and/or flights randomizations
  - Spectrum editing option (Rainflow, rise/fall, Dead band)
  - User-defined spectra (Afgrow format)
- Extreme Value Distribution
  - User input, e.g., Gumbel, Frechet , and Weibull.
  - Ultimate/Limit load (deterministic)
  - Computed from exceedance curves, weight matrix, etc. (Gumbel, Frechet , and Weibull)
- Probability calculations
  - POF (survival / no survival term)
  - Hazard fn. (with survival term)
  - Cumulative POF
- Crack growth
  - Direct Afgrow and Nasgro link
  - Through, Corner, Surface crack growth geometry options
  - Master curve for 2D (ai and Kc) interpolation (user input or developed from NASGRO/AFGROW)
  - Kriging for efficient probabilistic fracture analysis
- Probabilistic methods
  - Standard Monte Carlo
  - Numerical integration
  - Weighted Branch Integration Method
  - Remaining Useful Life Calculations
  - Importance Sampling
- Inspection capabilities
  - Any number of inspections (arbitrary limit set to 15)
  - Arbitrary repair crack size distribution (lognormal, tabular, Weibull, deterministic)
  - Arbitrary POD (lognormal, tabular)
  - Deterministic POD
  - User defined probability of inspection
  - Different repair scenarios within/between inspections
- Random variables
  - ai, Kc, Evd\_da/dN, hole diameter, hole offset
  - crack aspect ratio, yield stress, ultimate stress, loading
- Computational implementation
  - Standard Fortran 95/03/08, Windows and Unix (Intel ifort compiler)
  - HPC Implementation (parallel and vectorized)

